

How constraints refer to nothing: The correct notion of substructure for phonology Nick Danis^{1,3}, Jeffrey Heinz², and Adam Jardine³

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Overview

• Many markedness constraints identify illicit substructures of a representation Ex., *NC, *CODA, *[voice]



- The superstructure problem: a pattern in which a well-formed structure is a superstructure of an ill-formed one (Jardine and Heinz, in press; Jardine, 2016; Danis, 2017)
- We propose a strong (and mathematically natural) definition of substructure from logic and model theory that can capture these cases in a unified way and maintains a restrictive, negative conception of markedness

Negative Markedness

• From a logical perspective, the most restrictive constraints can only forbid substructures (Jardine and Heinz, in press)



 $\forall x, \exists y [+\text{nasal}](x) \rightarrow [-\text{voice}](y)$ "If there is a nasal, there must be a voiceless segment (somewhere in the word)"

• Example negative (string) literal:

 $\neg *NC$ "Don't contain a *NC sequence"

The Superstructure Problem

- Given non-linear representations, some constraints appear to **require** structure
- **Aghem** (Hyman, 2014)
 - When H tone is followed by L, it spreads to the right: a. $\dot{e} - n \delta m \to [\dot{e} - n \delta m]$ 'to be hot'

b. /fú - kìa/
$$\rightarrow$$
 [fú - kîa] 'your sg. rat'

c. e-nom \rightarrow e-nom [é - nôm] 'to be hot'

Η̈́L

- Constraint: "H must spread to a following L-toned mora"
- · The well-formed structure includes the ill-formed structure

• CODACOND (Ito 1986, Ito and Mester, 1994)

* $C]_{\sigma}C$

place

 $\sqrt{[CVC]_{\sigma}CV}$ place

- Other examples:
 - Ngbaka coocurrence restrictions on complex consonants (Sagey 1986, Danis 2017)
 - Spreading in Tingrinya and other languages (Hayes 1986)

Defining Substructure

- Substructure: For two structures A and B in S. A is a substructure of B iff there is a mapping h from D^A to D^B such that
 - for every unary relation R_i , $d^A \in R_i$ in A iff $h(d^A) \in R_i$ in *B*, and
 - for every binary relation R_i , $(d_1^A, d_2^A) \in R_i$ in A iff $(h(d_1^A), h(d_2^A)) \in R_i$ in B
- This definition is standard in logic and model theory (Libkin, 2004)
- This strong definition differs from earlier (for phonology) weak definition, which uses if instead (Hayes, 1986; Jardine and Heinz, in press; Jardine, 2017)

Aghem Tone Spreading



Discussion

- The strong definition is more expressive than the weak, but still **negative**
- Constraints like SPEC-T ("Syllables must be specified for tone"; Yip, 2002)) are different; they warrant further study

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• The mapping h from A to B satisfies the definition, but there is no such mapping from A to C• Thus, B is not grammatical for Aghem, but C is.



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